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Highlights

• A survey of the BWM based on the publications from 2015 to January 2019 is provided. • This paper intends to answer five questions about the BWM. • This paper has guiding significance for the later research related to the BWM.

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The state-of-the-art survey on integrations and applications of the best worst method in decision making: Why, what, what for and what's next?^{**}

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ABSTRACT

After the first paper regarding the Best Worst Method (BWM) was published in Omega in 2015 (J. Rezaei, Best-worst multi-criteria decision-making method, Omega 53 (2015) 49-57), it has attracted many scholars' attention due to the efficiency of this method in reducing the times of pairwise comparisons and the good performance in maintaining consistency between judgments. Lots of researches related to this method have been published over the past several years. This paper concentrates on the state-of-the-art survey of the BWM based on the in-depth analysis over the publications concerning this method published from 2015 to 26th, January 2019. This paper intends to answer five questions about the BWM: (1) How does this method perform in bibliometric analysis? (2) Why to propose this method and what is it? (3) Which integrations that the BWM were focused on and which areas did they apply to? (4) What extensions of this method were investigated? (5) What are the challenges and future research directions regarding this method? In view of the fact that the research on this method is still in infancy, this paper has guiding significance for the later research related to the BWM. From the theoretical point of view, the reasonable value of consistency ratio, the inconsistency improving methods, the uncertain extensions of the BWM and the techniques for solving multi-optimality model in the BWM are good research issues that need to be further investigated in the future. From the perspective of application, the software packages for this method, the various integrations of this method, the wider application areas, and the international cooperation on this method are good topics to consider.

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1 1. Introduction

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2 There is no denying that, as a vital and popular research 3 branch of decision-making theory, Multiple Criteria Decision Making (MCDM) has wined great success. The MCDM can be divided 4 into two categories: continuous MCDM, also called as Multiple Ob-5 jective Decision Making (MODM), and discrete MCDM, also named 6 7 as Multiple Attribute Decision Making (MADM). The major distinction between MODM and MADM is the number of alternatives un-8 der evaluation [1]. In MODM problems, the number of alternatives 9 is not predetermined and the alternatives are restricted by a set of 10 optimal objective constraints; while in MADM problems, the num-11 ber of alternatives is predetermined and limited. The relationships 12 among MCDM, MODM and MADM within the context of decision-13 making theory can be illustrated in Fig. 1. In the following, we use 14

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https://doi.org/10.1016/j.omega.2019.01.009 0305-0483/© 2019 Elsevier Ltd. All rights reserved. the item "MCDM" to represent "discrete MCDM (MADM)" because many scholars take these terms as interchangeable [1].

The MCDM methods help Decision-Makers (DMs) do rational decisions [2]. Basically, there are two categories of MCDM techniques involving either quantitative or qualitative criteria (for a collection of state-of-the-art surveys, please refer to Refs. [3,4]):

(1) Multi-attribute utility and value theories. This kind of meth-21 ods need to construct decision matrix over alternatives. Af-22 ter experts give evaluations of alternatives over criteria, the 23 rating of each alternative can be obtained by some aggrega-24 tion functions to combine the scores of the alternative on all 25 criteria with the weights of criteria. The typical techniques 26 of this categories include TOPSIS (Technique for Order of 27 Preference by Similarity to Ideal Solution) [5], UTA (UTilites 28 Additives) [6], VIKOR (VIse Kriterijumska Optimizacija kom-29 promisno Resenje in Serbian, multiple criteria optimization 30 compromise solution) [7,8], MULTIMOORA (MULTIplicative 31 Multi-Objective Optimization by Ratio Analysis) [9,10], and 32

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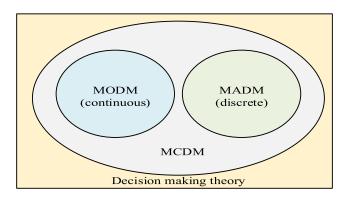


Fig. 1. Relationships among MCDM, MODM and MADM.

MACBETH (Measuring Attractiveness by a Categorical Based
 Evaluation TecHnique) [11].

35 (2) Outranking methods. Outranking methods are based on 36 pairwise comparisons among alternatives with respect to 37 each criterion. The outranking relations, which represent the 38 dominance degree of one alternative over others, are ac-39 quired by aggregating the pairwise comparisons. The widelyused outranking methods are ELECTRE (ELimination Et Choix 40 Traduisant la REalité in French, ELimination and Choice Ex-41 42 pressing the Reality) [12], PROMETHEE (Preference Ranking 43 Organization METHod for Enrichment Evaluations) [13], and GLDS (Gained and Lost Dominance Score) method [14,15]. 44

Although there are two categories of MCDM methods, gener-45 ally, the steps of the MCDM methods are often resemble, includ-46 in blem definition, criteria determination, decision matrix con-47 struction, criteria weight determination and ranking derivation. It 48 is natural that the selection of suitable MCDM methods is based 49 on the structure of problems. After defining the problem and deter-50 mining the criteria, establishing a decision matrix and determining 51 criteria weights are significant for any MCDM techniques. Suppose 52 53 that a MCDM problem consists of a finite set of *m* feasible alternatives $\{A_1, A_2, \dots, A_m\}$, whose scores are given with respect to a set 54 of criteria $\{C_1, C_2, \cdots, C_n\}$ and are denoted as s_{ij} for the *i*th alter-55 56 native over the *j*th criterion $(i=1, 2, \dots, m, j=1, 2, \dots, n)$. Then, a decision matrix *D* can be obtained as: 57

$$D = \begin{matrix} C_1 & C_2 & \cdots & C_n \\ S_{11} & S_{12} & \cdots & S_{1n} \\ S_{21} & S_{22} & \cdots & S_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ S_{m1} & S_{m2} & \cdots & S_{mn} \end{matrix}$$
(1)

Based on D, the ranking of alternatives can be derived by the 58 MCDM methods. Thus, how to establish a decision matrix is very 59 important, and the decision matrix would determine the degree 60 61 of reasonability of the final result. A straightforward way to con-62 struct a decision matrix is the pairwise comparison method that was originally proposed by Thurstone [16]. It is especially useful 63 when the scores of alternatives or stimulus on each criterion are 64 not easy to obtain. 65

AHP (Analytic Hierarchy Process) [17], as a special kind of 66 utility-based MCDM technique, determines the weights of criteria 67 via pairwise comparisons [16]. It decomposes a complex MCDM 68 problem into a multi-level hierarchic structure of goals, criteria, 69 sub-criteria (if necessary) and alternatives. It provides a fundamen-70 tal scale of relative magnitudes expressed in dominance units to 71 represent judgments in the form of pairwise comparisons. AHP 72 shows efficiency in the situation that providing the estimated 73 scores for candidate alternatives with respect to criteria is unfea-74 75 sible or meaningless but expressing the relative preferences of the alternatives and criteria by preference relations is possible [1]. It 76 is observed that different ways has been used to transform pair-77 wise comparisons into the elements of a decision matrix, for ex-78 ample, PROMETHEE [13] providing six types of functions to trans-79 form preference degrees into scores. AHP [17] uses the prioritiza-80 tion process to obtain the priorities of alternatives on each crite-81 rion and then a decision matrix could be established. However, 82 it is impossible to neglect the inconsistency in pairwise compar-83 ison matrix since inconsistency usually happens in practice [18]. 84 The inconsistency of the pairwise comparison matrix is the salient 85 drawback of AHP, which may lead to wrong or misleading results. 86 In addition, if there are a large number of criteria or alternatives, 87 the numerous workloads of pairwise comparisons would increase 88 the complexity of solving MCDM problems and also lead to the 89 decrease of consistency for pairwise comparisons. For instance, if 90 there are 6 criteria and 6 alternatives in a MCDM problem, 105 91 times of pairwise comparisons need to be done by experts. Al-92 though AHP is one of the most popular MCDM methods, the high 93 challenge in doing pairwise comparisons and the lack of consis-94 tency result in criticisms [1,18]. 95

Rezaei [1] pointed out that these numerous workload and com-96 plexity of experts are not necessary, and the reason for this lim-97 itation is resulted from the unstructured way of doing pairwise 98 comparisons. To fill this gap, Rezaei [1] proposed a new technique, 99 named the Best Worst Method (BWM), to do pairwise comparisons 100 in a structured way. Since the BWM appears, it has attracted many 101 scholars' attention and lots of researches regarding the BWM 102 been published. The paper published by Rezaei [1] in 2015 has now 103 turned out to be the third most cited article published since 2014 104 in Omega.¹ It is predicted that the research on BWM will keep in-105 creasing in the coming future. 106

This paper concentrates on the state-of-the-art survey of inte-107 grations and applications of the BWM in decision making. After 108 making a bibliometric analysis on the BWM-related publications, 109 we select 124 representative publications concerning the BWM 110 published from 2015 to 26th, January 2019 and analyze them in-111 depth. This paper intends to answer the following questions: (1) 112 how does the BWM perform in bibliometric analysis? (2) why to 113 propose and what is the BWM? (3) which integrations that the 114 BWM were focused on and which areas did they apply to? (4) 115 what extensions of the BWM were investigated? (5) what are the 116 challenges and future research directions regarding the BWM? In 117 view of the fact that the research on the BWM is still in infancy, 118 this article has guiding significance for the later research related to 119 the BWM. 120

The rest of this paper is organized as follows: Section 2 provides a bird's eye of the BWM based on bibliometric analysis. 122 Section 3 clarifies why to propose the BWM. Then, Section 4 describes what is the BWM. The integrations of the BWM and their applications are addressed in Section 5. Section 6 concentrates on the challenge and future research directions about the BWM. Some conclusions are listed in Section 7. 127

2. A bird's eye of the BWM based on bibliometric analysis

This section gives a general introduction to the basic information of the BWM related publications and also some bibliometric analysis in terms of co-citation networks of journals, publications and authors, and the co-occurrence network of keywords.

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2.1. Data source: publications related to the BWM

Since the first paper about the BWM was proposed by Rezaei 134 [1] in 2015 in *Omega*, we selected all publications related to the 135

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The country/region distributions by countries/regions and citations of the 124 publications.

	Country/Region	Number of publications	Citations in Google scholar
1	Iran	32(2)	240
2	China	30(1)	304
3	Netherlands	23(2)	889
4	India	12(3)	207
5	Turkey	5	6
6	Serbia	3(3)	96
7	Indonesia	3	0
8	Bosnia and Herzegovina	2(1)	44
9	Australia	2(1)	15
10	Algeria	2	22
11	Lithuania	1(5)	48
12	UK	1(3)	13
13	Malaysia	1(1)	34
14	Italy	1(1)	2
15	Spain	1(1)	2
16	Libya	1	12
17	Bangladesh	1	5
18	Canada	1	1
19	Lucknow	1	1
20	Chile	1	0
21	USA	0(4)	120
22	France	0(2)	22
23	Ghana	0(2)	50
24	Denmark	0(1)	38
25	Japan	0(1)	12
26	Saudi Arabia	0(1)	2
27	Germany	0(1)	0
	Subtotal	124	1746

Note: In the third column, the first number indicates the number of first author publications; the number in bracket indicates the number of non-first author publications.

BWM in Web of Science (WoS) published from 2015 to 26th, Jan-136 137 uary 2019 and there are 82 publications, including 78 journal papers and 4 conference papers. For a comprehensive study on the 138 BWM, Google scholar is an additional database since it is updated 139 140 much faster than WoS. Searching "best worst method" in Google scholar, 17 additional SCI (Sciences Citation Index) journal papers, 141 17 non-SCI journal papers, 5 conference papers, 1 case study, 1 142 chapter of handbook and 1 series of book series were obtained af-143 ter removing the aforementioned 82 publications that have been 144 retrieved from WoS. In total, these 124 publications include four 145 146 types: 112 journal articles, 9 conference papers, 1 case study, 1 chapter of handbook and 1 series of book series. There exists a reg-147 ular updated BWM bibliographical database,² provided by Rezaei. 148 149 Among these 112 journal publications, 95 publications were in-150 dexed by SCI database in WoS (78 of them have been indexed and the other 17 will be indexed soon). That is to say, 84.82% (95/112) 151 journal publications were published in SCI indexed journals. The 152 153 112 journal articles are summarized in Table A.1 in Appendix. This table shows that the 112 journals articles were published in 63 154 journals. It can provide some useful information for researchers to 155 156 submit their research manuscripts.

157 These 124 publications were distributed in 27 countries/regions (see Table 1). 28 publications were written in the form of interna-158 159 tional cooperation: 21 publications were written by authors from 160 two different countries/regions and 7 publications were written by 161 authors from three or more than three different countries/regions. In Table 1, if a country/region's author is not the first author of 162 a publication, then this publication will be counted separately. For 163 instance, Netherlands have 23 first-author publications, i.e., there 164 165 are 23 publications whose first authors are from Netherlands. The figure "2" in the bracket denotes that there is 2 publication that 166 167 finished by international collaboration, but the first author

was not from Netherlands. In total, Netherlands have 25 publica-168 tions in these 124 studies. As displayed in Table 1, Netherlands 169 takes the third position in the number of publications (25). 889 170 citations of Netherlands in Google Scholar accounts for almost 171 half of the sums of all 27 countries'/regions' citations (1746). This 172 is mainly because Rezaei, who proposed the BWM, comes from 173 Netherlands. Iran ranks first because of the largest number of pub-174 lications. Moreover, authors in China also pay much attention to 175 the BWM, similar numbers of publications as Iran but with more 176 citations. 177

2.2. Bibliometric analysis on the BWM-related publications in WoS

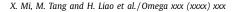
In the following, we use VOSviewer software package [19] to 179 analyze the publications listed in Table A.1. It is worth to note that 180 WoS database only could search the studies published in SCI in-181 dexed journals and the conference papers indexed by IEEE, and the 182 update time of WoS database is at the end time of each month. 183 Then, only 82 publications which contain 78 journal articles and 4 184 conference papers can be searched in WoS database. 16 SCI journal 185 articles cannot be searched in WoS database because the publica-186 tion time of these 16 SCI journal articles are just online and are not 187 retrieved in WoS. Based on these 82 BWM-related publications, we 188 use VOSviewer to draw four figures regarding co-citation networks 189 of journals, publications and authors, and the co-occurrence net-190 work of keywords. 191

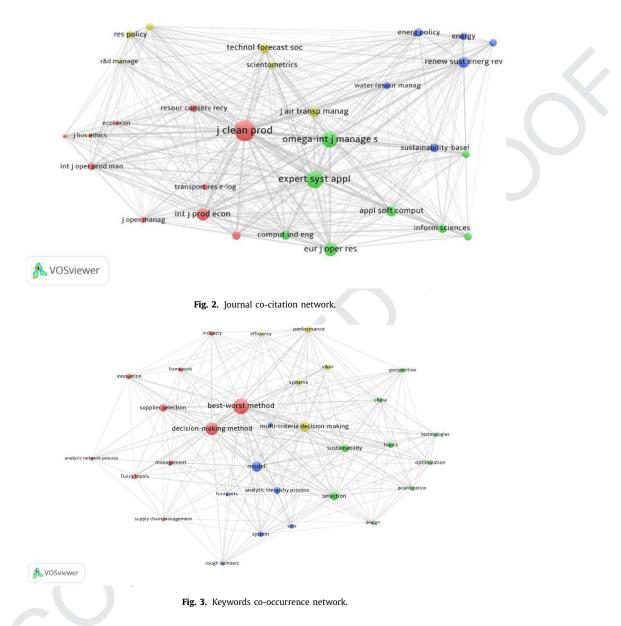
These are altogether 1676 journals that were cited by these 82 192 publications. We selected the top 30 journals to illustrate in Fig. 2. 193 In this figure, a node represents a journal. The size of the node 194 denotes the frequency of the journal cited by these 82 publica-195 tions. The grey lines show the relationships between journals. If 196 two nodes are appeared in the reference list in one paper at the 197 same time, then these two nodes establish a co-citation network. 198 The thickness of the line indicates the co-citation frequency. As is 199 demonstrated in Fig. 2, VOSviewer divides these journals into 4 200 clusters with different colors of nodes. Journal of Cleaner Production 201

² http://bestworstmethod.com/wp-content/uploads/2018/11/ BWM-bibliographical-database.pdf.

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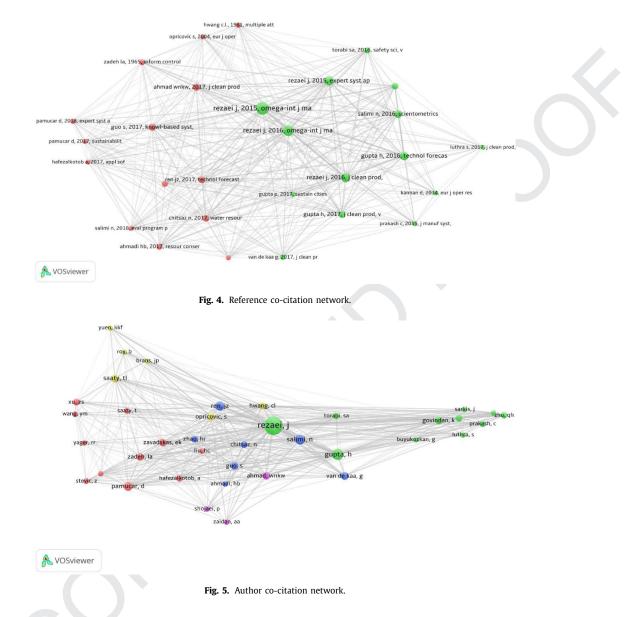
is the most popular journal with the maximal number of papers. 202 It is a top influential journal in the field of science & technology, 203 204 engineering and environmental science. According to the Journal Citation Reports (JCR) in 2017, it ranks 7/50 in the field of engi-205 neering and environmental, 21/241 in environmental sciences, 6/33 206 in green & sustainable, science & technology. Other influential jour-207 nals contain Omega, Expert Systems with Applications and European 208 Journal of Operational Research. These are very influential journals 209 210 in their fields, especially in management science and operations 211 research.

212 Before analyzing the keywords co-occurrence network, we pre-213 processed the data and merged the words with the same meaning 214 but in different forms before analyzing. For instance, four differ-215 ent keywords such as "best-worst method", "best worst method", "best worse method" and "bwm" represent the same meaning, so 216 they were merged into "best-worst method". In analogous, "multi-217 218 criteria decision making", "multi-criteria decision-making", "multi-219 criteria decision- making (MCDM)" were combined as "multi-220 criteria decision making"; "AHP" and "analytic hierarchy process" 221 were merged into "analytic hierarchy process"; "System" and "sys-222 tems" were processed as "system". The top 30 popular keywords of these 82 publications are shown in Fig. 3. From Fig. 3, we can find 223 that the "Best-worst method" is the most popular keyword. "De-224 cision making" and "Multi-criteria decision making" are two pop-225 ular keywords since BWM is a method to tackle decision-making 226 problems, especially the multi-criteria decision-making problems. 227 China is the only country whose name appears in keywords co-228 occurrence network. This may imply its leading position in the re-229 search direction of BWM. 230

The reference co-citation network shown as Fig. 4 illustrates the 231 most highly cited papers among these BWM-related publications. 232 In Fig. 4, a node represents a reference. The line is established 233 when two documents appeared in the reference list of a BWM 234 publication at the same time. The thickness of the line is propor-235 tional to the co-citation frequency. The first three popular publi-236 cations were all written by Rezaei, the father of BWM. In Google 237 Scholar, Ref. [1] has received 284 citations till 26th, January 2019. 238 BWM was later implemented in Ref. [20] and Ref. [20] has been 239 cited 129 times. The first application of BWM was shown in Ref. 240 [21] and Ref. [21] has been cited 112 times. These three papers 241 play a vital role in the development of BWM. In the future, these 242

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three papers would be also highly cited in researches related toBWM.

245 There are 3152 authors in total that were once cited by these 82 publications. As mentioned above, the first three highly cited 246 247 papers were written by Rezaei. As displayed in Fig. 5, the biggest node is Rezaei, which is consistent with the result of reference 248 co-citation analysis. Gupta has written seven papers about BWM 249 250 [22–28]. Gupta has applied BWM to overcome the barriers in buildings with respect to energy efficiency, and also in choosing 251 MSMEs (Micro-small and Medium Enterprises) and SMEs (Small 252 and Medium Enterprises). Ren [29-32] applied BWM to manage 253 254 polygeneration system, urban sewage sludge and technology se-255 lection for ballast water treatment. Salimi has written three papers [33–35] related to education area, research and development 256 performance of firms, and scientific outputs quality evaluation. 257 Based on the number of papers and the ranges of application area, 258 Gutpa, Ren and Salimi becomes the top popular authors just be-259 hind Rezaei. 260

261 3. Why to propose the BWM?

This section introduces the motivation of the BWM. The comparison between AHP and BWM is provided as well. In AHP, to compare the importance of *n* criteria, a reciprocity 264 preference relation shown below can be constructed based on the pairwise comparisons using Saaty's 1/9-9 scale [5]: 266

$$\mathbf{A} = \begin{pmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{pmatrix}$$

where a_{it} denotes the preference degree of criterion C_i over crite-267 rion C_t . Especially, $a_{it} = 1/9$ implies that criterion C_t is absolutely 268 preferred to criterion C_j ; $a_{jt} = 9$ implies that criterion C_j is abso-269 lutely preferred to criterion C_t ; $a_{it} = 1$ means that criterion C_i is 270 equally important to criterion C_t . In the pairwise comparison ma-271 trix A, a_{ti} can be derived by the reciprocity $a_{ti} = 1/a_{it}$. In addi-272 tion, for the 1/9–9 scale, the transitivity $a_{it} = a_{ik} \times a_{kt}$ holds for 273 274 any $i, t \in n$.

As an MCDM method, BWM was proposed by Razaei [1] to fill 275 the challenges of AHP in numerous pairwise comparisons and lacking of consistency. Razaei [1] gave the reason why AHP is criticized 277 for complexity of pairwise comparisons and low consistency. Inconsistency is unavoidable in pairwise comparisons due to the fact 279

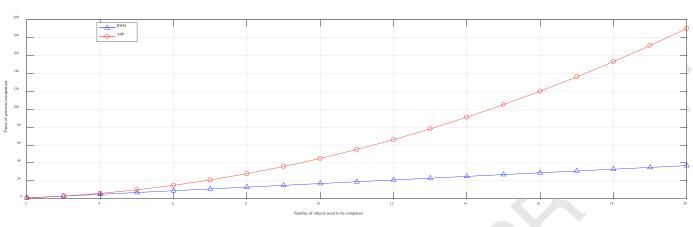


Fig. 6. The times of pairwise comparisons of BWM and AHP.

that the structure of doing pairwise comparisons in AHP is unrea-sonable [1,18].

To overcome these defects, Razaei [1] established a new struc-282 ture of doing pairwise comparisons. The best (the most important 283 or the most desirable) and the worst (the least important or the 284 least desirable) objects are the predefined benchmarks or refer-285 286 ences for all the rest objects. In the BWM, only reference comparisons are necessary. The concept of reference comparisons is that 287 288 the elements of pairwise comparisons should have at least a ref-289 erence, i.e., the worst or the best object. Experts only do reference comparisons in decision-making process. It forms a new structure 290 291 of pairwise comparisons in BWM, which is quite different from the pairwise comparisons in AHP. 292

In AHP, each criterion should be compared with all the other criteria. In this sense, for *n* criteria, using reciprocity, at least n(n-1)/2 pairwise comparisons need to be executed by expert. The n(n-1)/2 pairwise comparisons contains the reference comparisons and other comparisons which do not include the reference criteria. These other comparisons just lead to the inconsistent comparisons.

300 In the BWM, for *n* criteria, the best criterion C_B and the worst criterion C_W are predetermined by expert. Then, on the one hand, 301 the reference comparisons include the best criterion C_B with all the 302 other criteria except the best criterion C_B , i.e., $\{C_1, C_2, \dots, C_n\}/\{C_B\}$. 303 n-1 times of pairwise comparisons are done in the reference 304 305 comparisons regarding the best criterion C_B . On the other hand, 306 the reference comparisons regarding the worst criterion C_W consists the worst criterion C_W with all the other criteria except the 307 best criterion C_R and the worst criterion C_W because the compar-308 309 ison between the best criterion and the worst criterion has been 310 done in the process of the reference comparisons regarding the best criterion C_B , i.e., $\{C_1, C_2, \dots, C_n\}/\{C_B, C_W\}$. Hence, in the frame-311 work of BWM, we only need to do 2n - 3 times of pairwise com-312 parisons. It is worth to note that the information about the other 313 pairwise comparisons exclude the reference criteria could be de-314 315 rived by the known reference comparisons in BWM. Therefore, the 316 time of pairwise comparisons in BWM is 2n - 3 in total.

317 Fig. 6 clearly shows the difference in times of pairwise compar-318 isons between BWM and AHP. The X-axis is designed to denote the 319 number of objects to be compared in the decision-making process. The Y-axis refers to the times of pairwise comparisons using dif-320 ferent methods. The blue line represents the BWM and the mathe-321 matical function is f(n) = 2n - 3. While the red line denotes the 322 AHP and the mathematical function is f(n) = n(n-1)/2. When 323 324 the number of objects increases, the complexity of the BWM is linearly growing while the complexity of the AHP method increases 325 exponentially. This figure intuitively shows the better performance 326

of the BWM than the AHP in terms of decreasing the times of pairwise comparisons. 327

4. What is the BWM? 329

This section addresses what is the BWM. The clear steps of the330BWM, the consistency ratio for the BWM and the linear model for331the BWM are presented in details.332

4.1. The steps of the BWM 333

BWM uses five steps to derive the weights of criteria [1]. The 334 weights of alternatives on each criterion can be derived in the 335 same process. Hence, we focus on the solving process regarding 336 the weights of criteria. Below we summarize the five steps of the 337 BWM [1].

Step 2. Choose the best criterion C_B and the worst criterion C_W 340from the set of decision criteria. If there is more than one best cri-
terion or worst criterion, the best and worst criteria can be chosen
arbitrarily.341343343

Step 3. Do pairwise comparisons between the best criterion C_B and 344 the other criteria. Then, the Best to Others (BO) vector could be 345 established as: 346

$$BO = (a_{B1}, a_{B2}, \cdots, a_{Bj}, \cdots, a_{Bn})$$

$$\tag{2}$$

where a_{Bj} denotes the preference degree of the best criterion 347 C_B over criterion C_j , and $a_{Bj} \ge 1$, $j = 1, 2, \dots, n$; $j \ne B$. 348

Step 4. Do pairwise comparisons between the worst criterion C_W 349and the other criteria. Then, the Others to Worst (OW) vector could350be established as:351

$$OW = \left(a_{1W}, a_{2W}, \cdots, a_{jW}, \cdots, a_{nW}\right)^{\prime}$$
(3)

where a_{jW} denotes the preference degree of criterion C_j over 352 the worst criterion C_W , and $a_{jW} \ge 1$, $j = 1, 2, \dots, n$; $j \ne B$ or W. In 353 this step, n - 2 pairwise comparisons need to be done because a_{BW} 354 is known in the BO vector. It is worth to note that OW is a $n \times 1$ 355 vector. 356

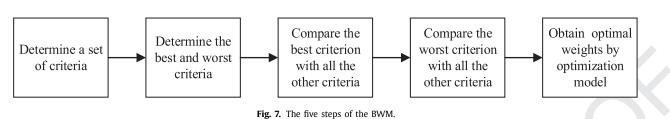
Step 5. Derive the weights of criteria by optimization models. For each reference comparison, the optimal weights of criteria satisfy $w_B/w_j = a_{Bj}$ and $w_j/w_W = a_{jW}$. Thus, the maximum absolute differences $|w_B/w_j - a_{Bj}|$ and $|w_j/w_W - a_{jW}|$ should be minimized. 360 Then, a min-max model (Model 1) could be established: 361

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362 Model 1 [1]

n

$$\min \max_{j} \left\{ \left| w_{B}/w_{j} - a_{Bj} \right|, \left| w_{j}/w_{W} - a_{jW} \right| \right\} \\ s.t. \quad \sum_{i=1}^{n} w_{i} = 1, w_{i} \ge 0, \ j = 1, 2, \cdots, r$$

Using ξ to denote the maximum absolute difference, Model 1 can be equivalently transformed into Model 2:

 $\min_{s.t.} \left| \begin{array}{c} \xi \\ \sum_{j=1}^{n} w_j = 1, w_j \ge 0, \ j = 1, 2, \cdots, n \\ \left| \begin{array}{c} w_B / w_j - a_{Bj} \right| \le \xi \\ w_j / w_W - a_{jW} \right| \le \xi \end{array}$

The solution space of Model 1 could be non-empty when the value of ξ takes an enough great value from mathematical point of view. Solving Model 2, the weights of criteria and the corresponding maximum absolute difference could be derived.

The five steps of the BWM can be summarized in Fig. 7.

- Generally, the BWM has three advantages over the AHP:
- 372 (1) One is the less times of comparisons in BWM than those 373 in AHP, because the BWM derives the weights of criteria 374 based on the vectors of pairwise comparisons shown as Eqs. (2) and (3) while the AHP utilizes the whole matrix 375 of comparisons. Based on the reciprocity and transitivity of 376 pairwise comparisons, after obtaining the reference compar-377 378 isons regarding the best criterion and the worst criterion, 379 the preference degrees among other criteria except the best 380 criterion and the worst criterion could be derived.
- (2) Secondly, in the structured comparing process of the BWM,
 only the integers, i.e., 1–9 scale, are used, while in the AHP,
 the 1/9–9 scale is used. In this regard, the complexity of
 comparisons reduces again. In addition, the integral grades
 are much closer to human perceptions and cognition, and
 this further makes the evaluation process much easier.
- (3) The third benefit is that the BWM has better performance in maintaining the consistency of pairwise comparisons since the redundant comparisons are eliminated. This makes the results derived by the BWM more reliable than those derived by the AHP. We shall further highlight this issue in Section 4.2.

We should note that scholars also proposed different for-393 394 mulas to model the deviation between w_B/w_i and a_{Bi} , and 395 the deviation between w_j/w_W and a_{jW} . For example, Brunelli and Rezaei [36] proposed the multiplicative norm of the devi-396 ation, shown as $\{a_{ij}/\frac{w_i}{w_j}, \frac{w_i}{w_j}/a_{ij}\}$. Unlike the Hamming distance 397 in the objective function of Model 1, Koçak, Çağlar and Öztaş 398 [37] proposed the Euclidean norm of the deviation, shown as 399 $\sqrt{(w_B/w_W - a_{BW})^2 + \sum_{j \neq W} (w_B/w_j - a_{Bj})^2 + \sum_{j \neq B} (w_j/w_W - a_{jW})^2}$ 400 However, it is observed that Model 1 is based on a min-max for-401 mulation. This formulation is one of the most important features 402 of the BWM, but this feature was neglected in Koçak, Çağlar 403 and Öztaş [37]'s model since the objective function is not in 404 min-max form any more. The min-max formulation guarantees 405 the consistency of each comparison in the BWM method, while 406 407 the model in Ref. [37] has a similar problem to AHP in terms of

consistency since both of them calculate the consistency of the 408 whole problem but do not care about the consistency between 409 individual comparisons. 410

4.2. The consistency ratio for the BWM

After obtaining the weights of criteria, the reliability of the results should be taken into consideration. ξ^* , obtained from Model 2, is the maximum absolute difference and it can be used in deriving the Consistency Ratio (CR). Intuitively, the greater the value of ξ^* is, the less reliable the comparisons are. Razaei [1] proposed a formula of CR for the BWM, shown as follows: 417

$$CR = \xi^* / Consistency \, Index$$
 (4)

where $CR \in [0, 1]$ and ξ^* is the maximum absolute difference derived from Model 2. The Consistency Index, denoted as ξ_{max} , is the maximum value of ξ when the greatest preference degree a_{BW} of criterion C_B over criterion C_W is determined.

The absolute consistency of a pairwise comparison matrix could 422 be justified as: for all *j*, $a_{Bj} \times a_{jW} = a_{BW}$ always holds. When the 423 condition $a_{Bj} \times a_{jW} = a_{BW}$ is not satisfied for some criteria C_j , the 424 consistency degree of the pairwise comparison matrix would de-425 crease. $a_{Bj} \times a_{jW} \neq a_{BW}$ has two conditions: $a_{Bj} \times a_{jW} > a_{BW}$ or 426 $a_{Bi} \times a_{iW} < a_{BW}$. The maximum value of ξ is resulted from the 427 maximum values of a_{Bj} and a_{jW} . When the condition $a_{Bj} = a_{jW} =$ 428 a_{BW} is true, the consistency degree of a pairwise comparison ma-429 trix has the smallest value. In this sense, the values of a_{Bi} and a_{iW} 430 should minus the value of ξ , and the value of a_{BW} should plus the 431 value of ξ : 432

$$(a_{Bj} - \xi) \times (a_{jW} - \xi) = a_{BW} + \xi \tag{5}$$

As for the highest inconsistency situation $a_{Bj} = a_{jW} = a_{BW}$, 433 Eq. (5) can be transformed to 434

$$(a_{BW} - \xi) \times (a_{BW} - \xi) = a_{BW} + \xi \tag{6}$$

Eq. (6) is a one-quadratic equation, with ξ being the variable 435 and a_{BW} being the constant parameter. 436

Solving Eq. (6), we can obtain two non-negative solutions of 437 Eq. (6) when the constant parameter a_{BW} is determined by expert. 438 Table 2 shows the small values of roots of Eq. (6). 439

Another group of large possible roots corresponding to differ-440 ent a_{BW} are 3.00, 4.56, 6.00, 7.37, 8.70, 10.00, 11.27, 12.53, 13.77, 441 respectively. In Table 2, there is only one kind of consistency index 442 values, corresponding to the small solution of Eq. (6), respectively. 443 Generally, the smaller the value of CR is, the better the consistency 444 of a pairwise comparison matrix should be. For the same max-445 imum absolute difference ξ_{max} of a pairwise comparison matrix, 446 the value of CR using the small possible root is greater than that 447 of the CR using the large possible root. Given that the maximal ab-448 solute deviation ξ_{max} should be smaller than the value of a_{BW} , the 449 large possible root should not be used to restrict the consistency 450 degree. It is reasonable and helpful to use the small possible root 451 as the Consistency Index ξ_{max} , i.e., the denominator of Eq. (4). 452

In Ref. [1], the value of Consistency Index is used in comparing 453 the consistency property of BWM with that of AHP. Rezaei [1] applied the BWM into a real-world problem concerning choosing mobile phone. The results derived from the BWM and the AHP were 456

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[m5G;February 4, 2019;13:40]

Table 2

The values of consiste	ency inde	ex.							
a _{BW}	1	2	3	4	5	6	7	8	9
Consistency Index	0.00	0.44	1.00	1.63	2.30	3.00	3.73	4.47	5.23

Table 3

Original cases and fuzzy consistency ratio.								
Case	BWM			Fuzzy BWM				
	ξ	CI	CR	ξf	CI-F	CR-F	CI-T	CR-T
Example 1 in Ref. [1]	0.260	4.47	0.0582	0.4495	8.04	0.0559	1.96	0.2293
Example 3 in Ref. [20]	1.000	4.47	0.2237	0.7913	8.04	0.0984	1.96	0.4037
Example in Ref. [21]	1.146	3.00	0.3820	0.2361	6.69	0.0353	1.31	0.1802

compared from four aspects: consistency ratio, minimum violation, 457 total deviation and conformity. In terms of these four aspects, the 458 459 BWM performs better than the AHP [1]. Generally speaking, the 460 BWM owns the advantages in requiring less times of comparisons 461 and obtaining more reliable and consistent results than the AHP.

Scholars have extended the BWM to fuzzy context. For the CR 462 under fuzzy conditions, Guo and Zhao [38] used three case studies 463 to show that the fuzzy extension of the BWM owns higher consis-464 465 tency ratio than the original BWM. In our perspective, this conclusion may be not true because different rules were used in these 466 methods to choose the consistency index and wrong consistency 467 index was chosen in fuzzy BWM. To clearly illustrate the differ-468 ence, we tabulate the important data of those three case studies 469 470 used in Refs. [1,20,21,38] in Table 3.

471 Given that Eq. (6) has two feasible solutions from mathematical point of view, in Refs. [1,20,21], the minimal solutions of Eq. (6), 472 473 called as CI-T (Consistency index-True), were chosen for strict consistency ratio. While in Ref. [38], the maximal solutions of Eq. (6), 474 475 named as CI-F (Consistency index-False), were taken in calculating the CR. If the maximal solutions of Eq. (6) were taken into 476 account, the CR-T (Consistency Ratio-True) in Ref. [38] would be 477 changed to 0.2293, 0.4037, 0.1802. In Example 1 in Ref. [1] and Ex-478 479 ample 3 in Ref. [20], the original BWM shows better than the fuzzy 480 BWM proposed in Ref. [38] in terms of CR. Only in the example of the comparisons of willingness [21], the fuzzy BWM performs 481 better than the original BWM. Even though the fuzzy extension of 482 the BWM may performs better as indicated by some scholars, we 483 should note that the original BWM has high consistency than the 484 fuzzy extensions of BWM because the fuzzy extensions of BWM 485 contains uncertain information which may result in inconsistency. 486

4.3. How to handle the multi-optimality of the weight determining 487 model in the BWM 488

After proposing the BWM [1], Razaei [20] further investigated 489 the multi-optimality of the BWM, and established a linear model 490 491 for the BWM from interval and linear aspects. In this section, we 492 address this model briefly.

Why do we need to transform the min-max non-linear 493 model into a linear model? Since the pairwise comparison is 494 not always fully consistent, multi-optimality could be derived from 495 Model 2. The multi-optimality of Model 2 could provide more in-496 497 formation than the singleton optimal solution. However, in some situations, decision-makers prefer the unique optimal solution. In 498 499 this case, Razaei [20] presented two ways to tackle this issue: one is based on interval analysis and the other is to convert the min-500 501 max non-linear model into a linear model.

How does the multi-optimality exist in the BWM? The rea-502 son of multi-optimality in Model 2 could be explained in terms 503 of linear algebra. The multi-optimality of Model 2 results from the 504 505 inconsistency of pairwise comparison matrix when the number of criteria is greater than three. In the case that the number of cri-506 teria is two, the pairwise comparison matrix is totally consistent 507 since $a_{Bi} \times a_{iW} = a_{BW}$ always holds. 508

In fully consistent situation, the inequality constraints can 509 be converted into corresponding equality constraints. For exam-510 ple, $|w_B/w_j - a_{Bj}| \le \xi$ can be converted to $w_B/w_j - a_{Bj} = 0$, and 511 $|w_j/w_W - a_{jW}| \le \xi$ can be converted to $w_j/w_W - a_{jW} = 0$. In addi-512 tion, the condition of $a_{Bj} \times a_{jW} = a_{BW}$ always holds in fully consis-513 tent situation. In this sense, there is only n-1 independent com-514 parison constraints and n - 1 comes from the number of criteria, n, 515 minus the criterion itself. Considering the constraint on the sum-516 mation of weights, there are n independent constraints with re-517 spect to *n* variables. Thus, in fully consistent situation, Model 2 has 518 a unique solution. 519

In not-fully consistent situation, each inequality constraint can 520 be converted into two corresponding constraints of inequali-521 ties. For example, $|w_B/w_j - a_{Bj}| \le \xi$ can be transformed to $w_B - \xi$ 522 $a_{Bj}w_j \le w_j\xi$ and $w_B - a_{Bj}w_j \ge w_j\xi$. Similarly, $|w_j/w_W - a_{jW}| \le \xi$ 523 can be converted into $w_j - a_{jW}w_W \le w_W \xi$ and $w_j - a_{jW}w_W \ge$ 524 $w_W \xi$. As we discussed previously, there are 2n - 3 pairwise com-525 parisons in the BWM. Hence, in not-fully consistent situation, 526 Model 2 has 4n - 5 constraints in total including the constraint on 527 the summation of weights. In addition, there are *n* variables of the 528 weights of criteria and 4n - 8 slack variables in Model 2. That is to 529 say, Model 2 has 5n - 8 variables in total. In linear algebra, if the 530 number of variables is greater than that of constraints in a model, 531 the model has multi-optimality. Then, we discuss the relations be-532 tween these 4n - 5 constraints and 5n - 8 variables. 533

Case 1. If the number of criteria is three, 4n - 5 = 5n - 8; 534

Case 2. If the number of criteria is greater than three, 4n - 5 < 3535 5n - 8, that is to say, the number of constraints is less than that of 536 variables. 537

Case 2 may lead to the multi-optimality of Model 2. 538 To solve this multi-optimality of Case 2, Rezaei [20] proposed 539 two models, i.e., Models 3 and 4, to obtain the interval weights of 540 criteria. 541 Мо 542

min w_i

s.t.
$$\sum_{j=1}^{n} w_j = 1, w_j \ge 0, \ j = 1, 2, \cdots, n$$
$$\begin{vmatrix} w_B/w_j - a_{Bj} \end{vmatrix} \le \xi^* \\ w_j/w_W - a_{jW} \end{vmatrix} \le \xi^*$$

Model 4 [20]

$$\begin{array}{l} \max \ w_{j} \\ \text{t.} \quad \sum_{j=1}^{n} w_{j} = 1, w_{j} \ge 0, \ j = 1, 2, \cdots, n \\ \left| w_{B}/w_{j} - a_{Bj} \right| \le \xi^{*} \\ w_{i}/w_{W} - a_{iW} \right| \le \xi^{*} \end{array}$$

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544 Models 3 and 4 are solved after obtaining the value of ξ^* from 545 Model 2. Then, the interval values of the weights of criteria can 546 be derived. If the pairwise comparison vectors are fully consistent, 547 the results of Models 3 and 4 are unique values and the intervals become crisp values. Therefore, the boundaries of Models 3 and 4 548 549 are reasonable.

Another approach to obtain the unique solution of Case 2 is 550 to transform the min-max model (Model 1) into a linear 551 552 model, by converting the initial min-max objective function min max{ $|w_B/w_i - a_{Bi}|, |w_i/w_W - a_{iW}|$ } into a linear min-max 553

objective function min $\max_{i} \{|w_B - a_{Bj}w_j|, |w_j - a_{jW}w_W|\}$. Then, 554

Model 2 can be rewritten as Model 5: 555 Model 5 [20]

556

min ξ^l

s.t. $\sum_{j=1}^{n} w_j = 1, w_j \ge 0, j = 1, 2, \dots, n$ $\begin{vmatrix} w_B - a_{Bj} w_j \end{vmatrix} \le \xi^L \\ w_j - a_{jW} w_W \end{vmatrix} \le \xi^L$

557 It is not difficult to find that Model 5 is a linear model, which leads to a unique solution. Solving Model 5, the unique solution 558 about the weights of criteria $w = (w_1, w_2, \dots, w_n)^T$ and the mini-559 mum absolute difference ξ^{L*} could be obtained. In Ref. [20], Rezaei 560 used several examples to prove that the unique solution of Model 561 5 is very close to the center of the interval weights of criteria de-562 563 rived from Models 3 and 4.

564 It is worth to note that, with the linear Model 5 of the BWM, Eq. (4) is replaced by the value of ξ^{L*} . The value of ξ^{L*} close to 565 zero means a minimal inconsistency of a pairwise comparison ma-566 567 trix.

5. Integrations of the BWM and their applications: What for? 568

The BWM, as a theoretical model, has been tested in real-life 569 570 applications. Among the 124 publications, 83 of them concerned the integrations of the BWM. Among these 83 publications, 40 571 of them concentrated on the singleton integrations of the BWM 572 and 43 of them integrated more than one method with the BWM. 573 In this section, we introduce the applications of the stand-alone 574 575 BWM, and the single integrations, multiple integrations and their corresponding applications, respectively. 576

5.1. Applications of the stand-alone BWM 577

Over the past years since the BWM was initially proposed in 578 2015, many researches related to the BWM have been published. 579 There are 41 publications focused only on the BWM. Table 4 shows 580 the applications of the stand-alone BWM. 581

5.2. Singleton integration of the BWM and their applications 582

583 There are 40 publications addressing the singleton integration 584 of the BWM, including 36 journal articles, 2 conference papers, 1 case study and 1 chapter of handbook. The most popular singleton 585 integrations of the BWM are listed in Table 5. 586

In Table 5, the most popular integration of the BWM is the un-587 certain condition. Two categories, fuzzy information [71-76] and 588 589 interval values [32,77,78], were used to combine with the BWM. 590 Fuzzy sets [71,74], triangular fuzzy number with membership func-591 tions [76], interval-valued multiplicative sets [72], probabilistic hesitant fuzzy sets [73] and Z-numbers [75], have been used to 592 represent uncertainty in the BWM. Anyway, we should note that 593 the interval weights, coming from the not-fully consistent non-594 linear BWM, are totally different from the interval used in the in-595 put data of fuzzy BWM. The former is valid since the weight is a 596 ratio scale, while the latter may be questionable as the 1-9 scale is 597

not a ratio scale. This is still an open question and more discussion 598 should be given in this regard in the future. 599

The second stream of the combination about the BWM is with 600 the TOPSIS method. Refs. [24-26,28,79,80] investigated the BWM 601 with the variants of the TOPSIS method. Gupta and Barua [24-602 26] focused on SMEs' supplier selection in terms of innovation 603 ability and overcame barriers of green innovation, respectively. 604 Gupta [28] used the BWM and the fuzzy TOPSIS method to eval-605 uate service quality of airline industry. You et al. [79] combined 606 the BWM with the TOPSIS method to evaluate the performances 607 of power grid enterprises to advocate the sustainable development. 608 Askarifar et al. [80] used the BWM and the TOPSIS method to eval-609 uate investment opportunities in a region. 610

Moreover, the VIKOR method has been combined with the 611 BMW in one journal paper [27] to evaluate service quality of air-612 line industry, one conference paper [81] to select web services 613 and one journal paper [82] regarding both strategic and opera-614 tional aspects of the selected criteria and proposed managerial im-615 plications, respectively. Garg and Sharma [83] focuses on the out-616 sourcing partner selection and evaluation. Furthermore, two papers 617 [86,87] focused on the combination of the fuzzy-Delphi method 618 with the BWM. 619

Except the popular singleton integrations of the BWM, there are 620 other singleton integrations of the BWM. These methods and their 621 corresponding applications are shown in Table 6. These singleton 622 integration of the BWM and their corresponding applications ap-623 peared in various kinds of publications, including 13 journal arti-624 cles, 1 conference paper, 1 chapter of handbook and 1 case study. 625 In Table 6, Bayesian network, fuzzy ANP, SAW and SERVQUAL are 626 useful approaches. In the future, these singleton integrations could 627 be mixed with other MCDM techniques to tackle complex decision-628 making problems. 629

5.3. Multiple integrations of the BWM and their applications

There are 43 publications which addressed the multiple integra-631 tions of the BWM. All of them are journal articles. Table 7 lists the 632 information of the 28 journal articles concerning two integrations 633 with the BWM and their corresponding applications. From Table 7, 634 it is not difficult to find that fuzzy logic and Group Decision Mak-635 ing (GDM) are two popular and interesting research issues with 636 the BWM. Multi-experts help to improve the quality of decision re-637 sult, which is an essential part in MCDM. Hafezalkotob and Hafeza-638 lkotob [14] used the fuzzy extension of the BWM to obtain the 639 weights of experts in GDM process. Mou et al. [104] adopted the 640 intuitionistic multiplicative weighted geometric aggregation oper-641 ator to get the collective evaluations about the GDM problem. 642 Mou et al. [105] first obtain the best and the worst criteria by 643 graph theory and acquired the collective evaluations after fusing 644 the acceptable consistency intuitionistic fuzzy preference relations 645 by intuitionistic fuzzy weighted aggregation operator. You et al. 646 [106] combined the ELECTRE III with intuitionistic multiplicative 647 and the interval-valued fuzzy BWM in GDM process. Safarzadeh, 648 Khansefid and Rasti-Barzoki [102] used the weights and perspec-649 tives of experts to acquire the best and the worst criteria. Then, 650 two mathematical models to deduce priorities and consistency ra-651 tio by two mathematical models. 652

In addition, there are 14 papers [105,106,129-140] which fo-653 cused on the combination with three or more than three tech-654 niques, shown in Table 8. Here we take several papers as a clar-655 ification. Ref. [135] combined the BWM with the QFD, fuzzy MUL-656 TIMOORA and fuzzy logic to evaluate the performance of smart 657 bike-sharing program. Ref. [137] combined the PHFLTS and PT to 658 fill the gap of the traditional QFD. In this paper, the customer re-659 quirements were converted into corresponding engineering char-660 acteristics and the weights of the customer requirements were de-661

10

Table 4

The applications of the stand-alone BWM.

Authors Year Applications areas Specific problems 2015 Rezaei [1] Manufacturing Mobile phone selection Rezaei et al. [21] 2015 Supplier development Link supplier development to supplier segmentation Sadaghiani et al. [39] Supply chain Evaluate external forces affecting supply chain sustainability in oil and gas industry 2015 sustainability Gupta and Barua [22] 2016 Micro-small and Identify enablers of technological innovation for Indian MSMEs medium enterprises Rezaei et al. [40] 2016 Supplier selection Evaluate a supplier selection life cycle Rezaei [20] 2016 Manufacturing Select Car Torabi et al. [41] 2016 Risk assessment An enhanced risk assessment framework for business continuity management systems Salimi and Rezaei [33] 2016 Education Measure efficiency of university-industry Ph.D. projects Ahmadi et al. [42] 2017 Supply chain Assess the social sustainability of supply chains Alhubaishy and 2017 Agile development Emotion influences on agile decision making Benedicenti [43] 2017 Key success factors evaluation in technological innovation development Ghaffari [44] Technology Gupta, Anand and 2017 Consumption of energy Develop a roadmap to overcome barriers to energy efficiency in buildings Gupta [23] Mohaghar et al. [45] 2017 Supply chain Appraise humanitarian supply chain risks Praditya and 2017 Sharing arrangements Assess factors' influencing information sharing arrangements Janssen[46] Rezaei et al. [47] 2017 Airline industry Complex bundling configurations in surface transportation of air freight Salimi [34] 2017 Quality assessment Assess quality of scientific outputs Kaa et al. [48] 2017 Biology Select biomass thermochemical conversion technology Ahmad et al. [49] 2017 Supply chain Evaluate the external forces affecting the sustainability of oil and gas supply chain Kaa et al. [50] 2017 Automotive The battle between battery and fuel cell powered electric vehicles Zhao et al. [51] 2017 Eco-industrial parks Comprehensive benefit evaluation of eco-industrial parks Salimi and Rezaei [35] 2018 Evaluate firms' R & D performance Performance evaluation Yadollahi et al. [52] 2018 Banking service Prioritize the factors of service experience in banks Technology Evaluate the most attractive technology in the R&D department of a high-tech company Kaa, Janssen and Rezaei 2018 [53] Rezaei et al. [54] 2018 Logistics Measure the importance of logistics performance indicators 2018 Kaa et al. [55] Energy Assign the relative importance to factors Moktadir et al. [56] 2018 Manufacturing Identify challenges for implementing Industry 4.0 Groenendijk, Rezaei 2018 Transportation Incorporate the travelers' experience value in assessing the quality of transit nodes and Correia [57] 2018 Rezaei et al. [58] Transportation Assess the port performance measurement Rezaei and Lajimi [59] 2018 Supply chain Realize combined purchasing portfolio matrix-supplier potential matrix segmentation Bonyani and 2018 Performance evaluation Evaluate foreign EPC companies Alimohammadlou [60] Sharma, Mangla and 2018 Transportation Evaluate the transportation challenges of the dairy industry Patil [61] Beemsterboer, Hendrix 2018 Manufacturing Mobile phone selection and Claassen [62] Rezaei et al. [63] 2018 Supply chain Evaluate the environmental, economic and social criteria for packaging Kusi-Sarpong, Gupta Supply chain Evaluate sustainable innovation criteria for sustainable supply chains in manufacturing companies 2018 and Sarkis [64] Vishnuprivan and 2018 Verification The BWM is used to verification for other methods Manoharan [65] 2018 Environment Obtain the objective and credible indicator weights Liu et al. [66] Zavadskas [67] 2018 Verification The BWM is used to verification for other methods 2018 Decide the significance and weighting criteria. Ajrina, Sarno and Mining Ginardi [68] Setyono and Sarno [69] 2018 Supply chain Evaluate performance and technical capability criteria Brunelli and Rezaei 2018 Mathematics Propose a way to denote the inconsistency deviation [36] Kaa et al. [70] 2019 Technology Compare relevant standard dominance factors of three types of communication technologies

termined by the BWM. Ref. [134] combined the BWM with three techniques, namely, TOPSIS, GRA and WSA. It aimed to test and optimize a turning operation. Ref. [138] used VIKOR, relative entropy and fuzzy BWM at the same time to do FMEA in manufacturing.

Based on the information in Tables 4–8, the application areas of the BWM can be summarized in Table A.3 in Appendix. It is not hard to find that supply chain is one of the most popular application areas of the BWM. Manufacturing, performance evaluation, airline industry, energy, transportation, education and technology are also widely applied areas of the BWM. The rest application areas may be popular soon after.

In total, for all 124 publications with respect to the BWM, Table 9 counts the number of publications by year about different kinds of integrations of the BWM. We can find that the number of singleton integration of the BWM is increasing by year and the 676 number of multiple integrations of the BWM is also raising. 677

6. Challenges and future research directions related to the 678 BWM: What's next? 679

The challenges and future research directions of the BWM can be discussed from theory aspect and application aspect, respectively. 682

From the perspective of theory, the reasonable values of CR, the inconsistency improving methods, the uncertain extensions of the BWM and the techniques to solve multi-optimality model in the BWM are good research issues that need to be further investigated. 686

Table 5

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Technique	Approach	Authors	Year	Applications areas
Uncertainty	Fuzzy information	Raj and Srivastava [71]	2018	Manufacturing
	Fuzzy information	Yang et al. [72]	2018	Education
	Fuzzy information	Li, Wang and Hu [73]	2018	Investment
	Fuzzy information	Torbati and Sayadi [74]	2018	Performance evaluation
	Fuzzy information	Aboutorab et al. [75]	2018	Supply Chain
	Fuzzy information	Khanmohammadi, Zandieh and Tayebi [76]	2018	Performance evaluation
	Interval analysis	Ren [32]	2018	Manufacturing
	Interval analysis	Ren et al. [77]	2018	Manufacturing
	Interval analysis	Sadjadia and Karimi [78]	2018	Manufacturing
TOPSIS	Fuzzy TOPSIS	Gupta and Barua [24]	2017	Supplier selection
	Fuzzy TOPSIS	Gupta and Barua [25]	2017	Supplier selection
	Fuzzy TOPSIS	Gupta and Barua [26]	2018	SMEs
	Fuzzy TOPSIS	Gupta [28]	2018	Performance evaluation
	TOPSIS	You et al. [79]	2017	Power Grid Enterprise
	TOPSIS	Askarifar et al. [80]	2018	Investment
VIKOR	VIKOR	Serrai et al. [81]	2016	Web Service
	VIKOR	Gupta [27]	2018	Airline industry
	VIKOR	Cheraghalipour, Paydar and Hajiaghaei-Keshteli [82]	2018	Supply Chain
	VIKOR	Garg and Sharma [83]	2018	Outsourcing adoption
	VIKOR	Liu, Hu and Zhang [84]	2018	Manufacturing
	VIKOR	Alsalem [85]	2018	Health care
FDM	Fuzzy-Delphi method	Nafari et al. [86]	2017	Higher education
	Fuzzy-Delphi method	Sahebi et al. [87]	2017	Humanitarian supply chain

Note: All abbreviations can find corresponding explanations in Table A.2 in Appendix.

Table 6

The other singleton integrations of the BWM and their corresponding applications.

Approach	Authors	Year	Application area	Specific problem
Expected marginal seat revenue	Joshi and Lohiya [88]	2016	Film/Movie Theatre	Increase revenue for movie theatre based on improved seating plans
PLS method	Sadeghi et al. [89]	2016	Supply Chain	Identify and prioritize contributing factors in supply chain competitiveness
Bayesian network	Abolbashari et al. [90]	2017	Procurement	Adjust the impact of each KPI on the procurement performance
Cognitive network process	Zhang et al. [91]	2017	Transportation	Select a freight transportation company
RIM	Sofuoğlu et al. [92]	2017	Turning operation	Optimize cut parameters
SWOT	Abadi et al. [93]	2018	Medical tourism	Evaluate medical tourism development strategy
SERVQUAL	Rezaei et al. [94]	2018	Quality assessment	Assess airline baggage handling systems' quality
K-means clustering	Kara and Firat [95]	2018	Supply chain	Supplier risk assessment
PROMETHEE II	Alimohammadlou and Bonyani [96]	2018	Food industry	Financial performance evaluation in Iran's food industry
RMCGP	Cheraghalipour and Farsad [97]	2018	Supply chain	Sustainable supplier selection and order allocation
ZOLP	Mokhtarzadeh et al. [98]	2018	Technology	Technology selection in information technology industry
ELECTRE III	Yadav et al. [99]	2018	Outsourcing adoption	Offshore outsourcing adoption
Euclidean BWM	Koçak, Çağlar and Öztaş [37]	2018	Manufacturing	Car selection
Markov chains	Nawaz et al. [100]	2018	Cloud service selection	Develop a cloud broker architecture
LSM	Safarzadeh and Rasti-Barzoki [101]	2018	Car selection	Select a car selection with four criteria and four alternatives
GDM	Safarzadeh, Khansefid and Rasti-Barzoki [102]	2018	Piping selection	Choose piping by four criteria: total cost, security, social costs and environmental costs
SWARA	Zolfani and Chatterjee [103]	2019	Materials selection	Choose the sustainable household furnishing materials

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(1) How to determine an acceptable value of CR in the BWM is still an open question. 0.1 is usually taken as a consistency threshold regarding the pairwise comparison matrix of Saaty [17]. However, in the BWM, less comparisons are required to execute and thus the BWM should have higher consistency than the AHP. There is no research about whether 0.1 is a suitable consistency threshold or not in the BWM. Statistical approach such as Monte Carlo stimulation may be a good technique to determine a reasonable value of CR in the BWM.

(2) The inconsistency repairing methods in uncertain situations of the BWM should be further investigated. Even though Rezaei [1] have provided a way to improve the inconsistent vectors of BWM, detailed inconsistency improving tech-700 niques in uncertain situations or in group decision making 701 scenario should be proposed for the reliability of final re-702 sults. On the condition that the consistency degree of a pair-703 wise comparison matrix is not high, the results derived from 704 this pairwise comparison matrix may be not reliable. Results 705 with low credibility or reasonability could not be utilized in 706 decision-making process. 707

(3) In uncertain situations, there are several papers about the fuzzy extensions of the BWM. Triangular fuzzy numbers, intuitionistic fuzzy numbers, interval-valued fuzzy numbers and rough numbers have been investigated with the BWM 711 in indeterminate environment. Based on these initial combi-712

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Table 7

The integrations of the BWM with two techniques and their corresponding applications.

Approach	Authors	Year	Applications area	Specific problem
SWOT/AHP	Chitsaz and Azarnivand	2017	Water management	Water scarcity management in arid regions
Fuzzy BWM/GMIR	Guo and Zhao [38]	2017	Transportation	Select optimal transportation mode to deliver products
Fuzzy BWM/GDM	Hafezalkotob and Hafezalkotob [108]	2017	Investment	Investment decision process of innovation projects
Intuitionistic fuzzy multiplicative BWM/GDM	Mou et al. [104]	2017	Healthcare management	Evaluation of severity of patients infected with emphysema
MAIRCA/Rough numbers and fuzzy information	Pamučar et al. [109]	2017	Location selection	Select location for wind farms
Extension theory/Combined weights	Ren [30]	2017	Technology selection	Technology selection for ballast water treatment by multi-stakeholders
TOPSIS/SAW	Ren et al. [31]	2017	Technology selection	Sustainability assessment of technologies
Fuzzy BWM/Interval TOPSIS	Wang et al. [29]	2017	Polygeneration	Develop a method for sustainability assessment of polygenerations
TLF/VIKOR	Fatrias et al. [110]	2017	Supply Chain	Obtain a compromised supplier ranking list
Rough BWM/SAW	Stević et al. [111]	2017	Location selection	Rationalize of logistics activities and processes for wagons selection
MABAC/interval-valued fuzzy-rough numbers	Pamučar et al. [112]	2018	Airline industry	Evaluate fire fighting aircraft
TLF/VIKOR	Shojaei et al. [113]	2018	Airline industry	Airports evaluation and ranking
Fuzzy BWM/Fuzzy ANP	Alimohammadloua and Bonyani [114]	2018	Manufacturing	Performance evaluation of companies in product development
Fuzzy TOPSIS/Fuzzy MOLP	Lo et al. [115]	2018	Supply chain	Green supplier selection and order allocation
Entropy methods/RIM	Sofuoğlu [116]	2018	Manufacturing	Material and process selection in engineering environment
WASPAS/MULTIMOORA	Hafezalkotob et al. [117]	2018	Agriculture	Determine the weights of criteria about olive harvesting machines
Fuzzy BWM/COPRAS	Mahdiraji et al. [118]	2018	Building	Analyzing key factors of sustainable architecture
FMEA/Linguistic distribution assessment	Nie et al. [119]	2018	Water management	Risk evaluation of supercritical water gasification system
FDM/VIKOR	Zhao, Zhao and Guo [120]	2018	Performance evaluation	Assess the performances of electricity grid corporations
ELECTRE III/PROMETHEE II	Bonyani and Alimohammadlou [121]	2018	Performance evaluation	Prioritize foreign companies in post-sanctions Iranian energy sector
Rough BWM/Rough SAW	Stević et al. [111]	2018	Transportation	Evaluate potential locations for roundabout construction
Rough BWM/MAIRCA	Badi and Ballem [122]	2018	Supply chain	Identify suppliers in pharmaceutical industry
2-tuple linguistic BWM/QFD	Mei, Liang and Tu [123]	2018	Emergency routes evaluation	Choose the emergency route in the Wuhan metro station
Fuzzy BWM/AD	Maghsoodi et al. [124]	2018	Product design	Evaluate aesthetic, practical, technical and cost criteria
DEA/PROMETHEE II	Alimohammadlou and Bonyani [125]	2018	Performance evaluation	Weight the financial ratios
Fuzzy BWM/MACBETH	Pourhejazy, Sarkis and Zhu [126]	2018	Product deletion	Evaluate criteria for product deletion of fast-consuming goods
SWOT/QFD	Vahidi, Torabi and Ramezankhani [127]	2018	Supply chain	Find the weight vector of each supplier' resilience score
AQM/FMEA	Liu et al. [128]	2018	Water treatment plant	Obtain the weights of risk factors

Table 8

The integrations of the BWM with three or more than three techniques and their applications.

Approach	Authors	Year	Applications areas
Intuitionistic multiplicative BWM/ ELECTRE III/GDM	You et al. [106]	2016	Location selection
AHP/VIKOR/SAW/TOPSIS/COPRAS	Serrai et al. [133]	2017	Web service selection
TOPSIS/GRA/WSA	Sofuoğlu and Orak [134]	2017	Turning operations
Intuitionistic fuzzy BWM /Graph theory/GDM	Mou et al. [105]	2017	Healthcare management
QFD/Fuzzy MULTIMOORA/Fuzzy BWM/Maximizing deviation method	Tian et al. [135]	2018	Smart bike-sharing program
SAW/TOPSIS/COPRAS	Sotoudeh-Anvari et al. [136]	2018	Search problem
PHFLTS/PT/QFD	Huang et al. [137]	2018	Manufacturing
VIKOR/Relative entropy/Fuzzy BWM	Tian et al. [138]	2018	Manufacturing
Linguistic distribution assessment/TOPSIS/DEMATEL	Nie et al. [139]	2018	Water management
Entropy/QFD/Fuzzy MULTIMOORA	Liu et al. [129]	2018	Supply chain
Entropy/CPT/Grey theory	Zhao, Guo and Zhao [140]	2018	Energy
Fuzzy BWM/TOPSIS/Taguchi method/Neutral network	Omrani, Alizadeh and Emrouznejad [130]	2018	Energy
Interval rough BWM/WASPAS/MABAC	Pamucara, Chatterjee and Zavadskasc [131]	2018	Logistics
FDM/Entropy weight determination method/VIKOR	Zhao, Guo and Zhao [132]	2018	Energy
Interval BWM/Interval MULTIMOORA method/Interval Borda rule	Hafezalkotob et al. [141]	2019	Vehicle engine selection

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Table 9 number of publications during 2015_2010 (January)

me num	ber of publication	lis during 2015-2	019 (January).		
Years	Number of publications				
	Stand-alone BWM	Singleton integration	Multiple integrations		
2015	3	1	-	3	
2016	5	4	1	10	
2017	12	8	13	33	
2018	20	27	28	75	
2019	1	1	1	3	
Total	41	40	43	124	

nations, the future research should focus on the membership 713 functions of fuzzy numbers. Hesitant fuzzy number shows 714 good performance in representing uncertain information by 715 using a set of possible values to characterize the member-716 717 ship degree. Moreover, linguistic variables and linguistic expressions are expedient when the cost to obtain numbers 718 is too high. Hence, hesitant fuzzy information and linguistic 719 720 information with membership functions (hesitant fuzzy lin-721 guistic information and probabilistic linguistic information) 722 are good research points with the BWM extensions. Given that uncertainty may lead to higher inconsistency, the incon-723 sistency improving process and the corresponding CR should 724 725 be determined in uncertain situation as well.

726 (4) The way to solve multi-optimality model in the BWM was as 727 follows: Rezaei [20] converted the original non-linear model 728 (Model 1) into a linear model (Model 5) and used two mod-729 els (Models 3 and 4) to calculate the upper and lower bound 730 of the interval weights. Rezaei [20] thought that the central value of interval weight is close to the solution of the lin-731 ear model based on three numerical examples. There is a 732 lack of proof of release between the central value of inter-733 val weight solutions of the Model 2 and the unique weight 734 solutions of Model 5 from mathematical perspective. Other 735 736 possible techniques to analyze the multi-optimality of Model 2 are interesting and challengeable. 737

From the perspective of application, the software package for 738 739 the BWM, the various integrations of the BWM, the different application areas and the international cooperation on the BWM are 740 good topics to consider in the future. 741

(1) There is a necessary to develop the software packages for the 742 743 BWM. Software packages of the BWM would contribute to reducing complexity of calculation and accelerating the presenta-744 tion of results. The software package of the BWM helps people 745 use the BWM in practice efficiently and widely. Actually Rezaei 746 747 provides an excel solver³ for calculating weights by using the linear models in Ref. [20]. Many MCDM methods, such as AHP, 748 ELECTRE and PROMETHEE have their corresponding software 749 packages, which are more flexible than the excel solver. Thanks 750 to the availability and effectivity of their software packages, 751 752 these MCDM methods are being used more and more widely. 753 If an excellent software package of the BWM is developed, the 754 applications related to the BWM would also become popular.

The integrations of the BWM should be enriched. Until now, 755 (2)33.06% (41/124) publications used the stand-alone BWM into 756 757 applications. Given that the BWM shows excellent performance 758 in deriving weights of criteria, other MCDM techniques without 759 weight-deriving process can be combined with the BWM, such 760 as TODIM [142]. Multiple integrations combining other useful techniques and the BWM to tackle complex decision-making problems are also potential research areas.

(3) The application areas of the BWM can be extended. Supply 763 chain is a popular application area with the BWM currently. 764 Other application areas, such as artificial intelligence, robots 765 choose for "Industry 4.0" strategy and big data analyze, are 766 good application areas [143]. 767

(4) Scholars who focus on the BWM should strengthen interna-768 tional cooperation. Only 16.93% (21/124) publications came 769 from two countries'/regions' collaboration and only 7 publica-770 tion came from three or more than three countries'/regions' 771 collaboration. It is noted that some publications' citations are 772 zero. International cooperation with scholars from other coun-773 tries/regions may improve the quality of publications and in-774 crease citations of publications to some extent. 775

7. Conclusion

Among the MCDM methods, AHP is a most extensively used ap-777 proach. However, AHP suffers from various drawbacks, such as the 778 redundant pairwise comparisons and the lack for consistency. The 779 BWM is designed to overcome the disadvantages of AHP. Given the 780 less pairwise comparisons and the high consistency of the pairwise 781 comparison matrix in the BWM that those in AHP, the BWM will 782 be as popular as AHP soon after. To identify the status and trends 783 of research related to the BWM and help researchers to improve 784 future researches, a state-of-the-art survey of researches related to 705 the BWM was conducted in this paper. Given that the BWM just has been proposed in three years, there are only 124 publications 787 related to the BWM. We reviewed the contents of these 124 pub-788 lications. Firstly, we summarized the journals and authors' coun-789 tries/regions related to the BWM publications. Then, bibliometric 790 analysis with respect to BWM publications in WoS database was 791 done based on the VOSviewer software package. After that, why to 792 propose the BWM and what is the BWM were answered. Later, var-793 ious integrations and applications of the BWM were summarized 794 to help researchers extract quick information. Furthermore, we in-795 troduced the extensions of the BWM from fuzzy logic and group 796 decision making aspects. Finally, the challenge and future research 797 directions related to the BWM were analyzed in detail. 798

In future, researches of the BWM could be carried from theo-799 retical level and application level in-depth. For the BWM itself, the 800 acceptable consistency ratio value and the inconsistency improv-801 ing methods can be addressed. The BWM within other contexts, 802 uncertainty or multigranularity, could be investigated. The multi-803 optimality solution of the model in the BWM could be solved from 804 other perspectives. For applications with the BWM, the software 805 package of the BWM should be developed. The multiple integra-806 tions of the BWM should be studied and the other application ar-807 eas could be extended. 808

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³ http://bestworstmethod.com/software/.

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819 Appendix

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Table A.1 Summary of the BWM-related journal articles published from 2015–2019 (January).

lo.	Journal name	SCI or not	No. of articles	Authors	Year
	Journal of Cleaner Production	\checkmark	10	Rezaei et al. [40]	2016
	-	·		Gupta and Barua [24]	2017
				Kaa et al. [48]	2017
				Ahmad et al. [49]	2017
				Wang et al. [29]	2017
				Tian et al. [135]	2018
				Lo et al. [115]	2018
				Nie et al. [139]	2018
				Omrani, Alizadeh and Emrouznejad	
				[130]	2018
				Vahidi, Torabi and Ramezankhani [127]	2018
2	Sustainability	\checkmark	8	Pamučar et al. [109]	2017
				You et al. [79]	2017
				Kara and Firat [95]	2018
				Mahdiraji et al. [118]	2018
				Zhao, Zhao and Guo [120]	2018
				Liu et al. [129]	2018
				Stević et al. [144]	2018
				Liu et al. [66]	2018
6	Decision Science Letters	X	Y	Ghaffari [44]	2017
				Abadi et al. [93]	2018
				Askarifar et al. [80]	2018
				Alimohammadloua and Bonyani [114]	2018
				Yadollahi et al. [52]	2018
				Sotoudeh-Anvari et al. [136]	2018
				Sadjadia and Karimi [78]	2018
Į	Computers & Industrial Engineering	1	5	Mou et al. [105]	2017
	computers & mudstriar Engineering	\sim	5	Cheraghalipour and Saba [97]	2018
				Safarzadeh, Khansefid and	2018
				Rasti-Barzoki [108]	
				Pamucara, Chatterjee and Zavadskasc [131]	2018
				Maghsoodi et al. [124]	2018
5	Symmetry	./	5	Yang et al. [72]	2016
	Symmetry	v	5	You et al. [106]	2016
				Stević et al. [111]	2010
				Mei, Liang and Tu [123]	2018
				Zolfani and Chatterjee [103]	2019
5	Expert Systems With Applications	\checkmark	4	Rezaei et al. [21]	2015
				Pamučar et al. [112]	2018
				Aboutorab et al. [75].	2018
				Pourhejazy, Sarkis and Zhu [126]	2018
	Energies	\checkmark	3	Kaa et al. [50]	2017
	5	•		Zhao, Guo and Zhao [140]	2018
				Zhao, Guo and Zhao [132]	2018
	International Journal of Production Research	/	3	Yadav et al. [99]	2018
	International journal of Froduction Research	\sim	5		
				Huang et al. [137]	2018
				Kusi-Sarpong, Gupta and Sarkis [64]	2018
	Journal of Air Transport Management	\checkmark	3	Rezaei et al. [47]	2017
				Gupta [27]	2018
				Shojaei et al. [113]	2018
0	Knowledge-Based Systems	\checkmark	3	Guo and Zhao [38]	2017
	~ .	•		Nie et al. [119]	2018
				Nawaz et al. [100]	2018
	Technological Forecasting & Social Change	\checkmark	3	Gupta and Barua [22]	2016
1	icennological forecasting & social challge	\sim		Ren et al. [31]	2010
l					2017 2018
l				Kaa, Janssen and Rezaei [53]	
		,			
	Applied Soft Computing	\checkmark	2	Hafezalkotob and Hafezalkotob [108]	2017
	Applied Soft Computing	\checkmark	2		
2	Applied Soft Computing Environment, Development and Sustainability	\checkmark	2 2	Hafezalkotob and Hafezalkotob [108]	2017
2				Hafezalkotob and Hafezalkotob [108] Tian et al. [138]	2017 2018
1 2 3 5	Environment, Development and Sustainability International Journal of Logistics Research and			Hafezalkotob and Hafezalkotob [108] Tian et al. [138] Zhao et al. [51]	2017 2018 2017
2 3	Environment, Development and Sustainability	\checkmark	2	Hafezalkotob and Hafezalkotob [108] Tian et al. [138] Zhao et al. [51] Garg and Sharma [83]	2017 2018 2017 2018
2 3	Environment, Development and Sustainability International Journal of Logistics Research and	\checkmark	2	Hafezalkotob and Hafezalkotob [108] Tian et al. [138] Zhao et al. [51] Garg and Sharma [83] Gupta and Barua [25]	2017 2018 2017 2018 2017

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Table A.1 (continued)

	ontinued)				
No.	Journal name	SCI or not	No. of articles	Authors	Year
				Liu, Hu and Zhang [84]	2018
17	Omega	\checkmark	2	Rezaei [1]	2015
18	Scientometrics	/	2	Rezaei [20] Salimi and Rezaei [33]	2016 2016
10	scientometrics	\checkmark	2	Salimi [34]	2010
19	Aiche Journal	\checkmark	1	Ren et al. [77]	2018
20	Accounting and Financial Control	x	1	Alimohammadlou and Bonyani [96]	2017
21	American Journal of Finance and Accounting	×	1	Alimohammadlou and Bonyani [125]	2018
22	Anadolu University Journal of Science & Technology A-	x	1	Sofuoğlu et al. [92]	2017
1 2	Applied Sciences & Engineering	/	1	Dai and Crivastava [145]	2019
22 23	Benchmarking: An International Journal Case Studies on Transport Policy	\checkmark	1 1	Raj and Srivastava [145] Groenendijk, Rezaei and Correia [57]	2018 2018
23	Chemosphere	\sim	1	Ren [30]	2018
25	Computers and Electronics in Agriculture	\sim	1	Hafezalkotob et al. [117]	2018
26	Decision Making: Applications in Management and Engineering	×	1	Badi and Ballem [122]	2018
27	Energy Strategy Reviews	\checkmark	1	Bonyania and Alimohammadlou	2018
28	Evaluation and Program Planning	\checkmark	1	Salimi and Rezaei [35]	2018
29	Global Journal of Flexible Systems Management	×	1	Khanmohammadi, Zandieh and Tayebi [76]	2018
30	IEEE Transactions on Reliability	\checkmark	1	Liu et al. [128]	2018
31 32	IEEE Transactions on Cybernetics Information Sciences	\sim	1	Hafezalkotob et al. [141] Mou et al. [104]	2019 2017
33	International Journal of Applied Decision Sciences	×	1	Cheraghalipour, Paydar and Hajiaghaei-Keshteli [82]	2017
34	International Journal of Construction Management		1	Bonyani and Alimohammadlou [60]	2018
35	International Journal of Disaster Risk Reduction	N. A.	1	Sahebi et al. [87]	2017
36	International Journal of Energy Research	$\overline{\mathbf{v}}$	1	Ren [32]	2018
37	International Journal of Information Technology & Decision Making	\checkmark	1	Koçak, Çağlar and Öztaş [37]	2018
38	International Journal of Intelligent Systems and Applications in Engineering	×	1	Sofuoğlu and Orak [134]	2017
39	International Journal of Machine Learning and Cybernetics	\checkmark	1	Li, Wang and Hu [73]	2018
40	International Journal of Social, Behavioral, Educational, Economic, Business and Industrial Engineering	X	1	Mohaghar et al. [45]	2017
41	Journal of Computational Science	./	1	Serrai et al. [133]	2017
42	Journal of Decision Systems	\sim	1	Safarzadeh and Rasti-Barzoki [101]	2018
43	Journal of Environmental Management		1	Gupta [28]	2018
44	Journal of Medical Systems	\checkmark	1	Alsalem [85]	2018
45	Journal of Soft Computing and Decision Support Systems	×	1	Torbati and Sayadi [146]	2018
46	Management Decision	\checkmark	1	Rezaei et al. [58]	2018
47	Operations Research Letters	\checkmark	1	Brunelli and Rezaei [36]	2018
48	Packaging Technology and Science Process Safety and Environmental Protection	\checkmark	1 1	Rezaei et al. [63] Moktadir et al. [56]	2018
49 50	Renewable and Sustainable Energy Reviews	\sim	1	Moktadir et al. [56] Kaa et al. [70]	2018 2019
51	Renewable Energy	$\tilde{\mathbf{v}}$	1	Vishnupriyan annd Manoharan [65]	2019
52	Resources, Conservation and Recycling	Ž.	1	Ahmadi et al. [42]	2017
53	Safety Science		1	Torabi et al. [41]	2017
54	SAGE Open	\checkmark	1	Nafari et al. [86]	2017
55	Science of the Total Environment	\checkmark	1	Gupta and Barua [26]	2018
56	Studies in Informatics and Control	\checkmark	1	Zavadskas [67]	2018
57	Sustainable Cities and Society	\checkmark	1	Gupta, Anand and Gupta [23]	2017
58	Technologies	\checkmark	1	Mokhtarzadeh and Mahdiraji [98]	2018
59 60	Technology Analysis & Strategic Management	$\overset{\checkmark}{\mathbf{v}}$	1	Kaa et al. [55]	2018
60 61	The Online Journal of Science and Technology Tourism Management	^	1 1	Sofuoğlu [116] Rezzei et al. [94]	2018 2018
62	Transport Policy	N/	1	Rezaei et al. [94] Rezaei et al. [54]	2018
63	Water Resources Management	$\sqrt[n]{}$	1	Chitsaz and Azarnivand [107]	2018
Subtotal		v 112	-		

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Table A.2Abbreviations and explanations.

Abbreviation	Explanation
AD	Axiomatic Design
AHP	Analytic Hierarchical Process
ANP	Analytic Network Process
AOM	Alternative Queuing Method
BWM	Best Worst Method
COPRAS	COmplex PRoportional ASsessment
CPT	Cumulative Prospect Theory
DEMATEL	DEcision MAking Trial and Evaluation Laboratory
EDAS	Evaluation based on Distance from Average Solution
ELECTRE	ELimination Et Choix Traduisant la REalité in French, ELimination and Choice Expressing the Reality
FDM	Fuzzy-Delphi Method
FMEA	Failure Mode and Effects Analysis
GDM	Group Decision Making
GMIR	Graded Mean Integration Representation
GRA	Grey Relational Analysis
IVFRN	Interval-Valued Fuzzy-Rough Numbers
LSM	Lexicographic Semi-order Model
MABAC	Multi-Attributive Border Approximation area Comparison
MADM	Multiple Attribute Decision Making
MAIRCA	Multi-Attributive Ideal-Real Comparative Analysis
MCDM	Multiple Criteria Decision Making
MODM	Multiple Objective Decision Making
MOLP	Multi-Objective Linear Programming
MULTIMOORA	Multi-Objective Optimization by Ratio Analysis plus the full MULTIplicative form
PHFLTS	Proportional Hesitant Fuzzy Linguistic Term Sets
PLS	Partial Least Squares
PROMETHEE	Preference Ranking Organization METHod for Enrichment of Evaluations
PT	Prospect Theory
QFD	Quality Function Deployment
RIM	Reference Ideal Method
RMCGP	Revised Multi-Choice Goal Programming
SAW	Simple Additive Weighting
SERVQUAL	SERVice QUALity
SWARA	Step-wise Weight Assessment Ratio Analysis
SWOT	Strengths, Weaknesses, Opportunities and Threats
TLF	Taguchi Loss Function
TOPSIS	Technique for Order Performance by Similarity to Ideal Solution
VIKOR	Vlse Kriterijumska Optimizacija kompromisno Resenje, in Serbian (multiple criteria optimization compromise solution)
WASPAS	Weighted Aggregated Sum Product Assessment
WSA	Weighted Sum Approach
ZOLP	Zero or One Linear Programming

Table A.3

Summary of the applications of the BWM and its extensions.

Application areas	Approaches	No of publications	References
Supply chain	Z number/BWM	24	Aboutorab et al. [75]
	Bayesian Network/BWM		Abolbashari et al. [90]
	BWM		Ahmadi et al. [42]
	Fuzzy TOPSIS/BWM		Gupta and Barua [24]
	BWM		Mohaghar et al. [45]
	BWM		Rezaei et al. [40]
	BWM/PLS method /BWM		Rezaei et al. [21]
	FDM/BWM		Sadaghiani [39]
	BWM		Sadeghi et al. [89]
	K-means clustering analysis/BWM		Sahebi et al. [87]
	TOPSIS/Fuzzy MOLP/BWM		Ahmad et al. [49]
	RMGP/BWM		Kara and Firat [95]
	TLF/VIKOR/BWM		Lo et al. [115]
	VIKOR/Sensitive analysis/BWM		Cheraghalipoura and Farsad [97]
	Fuzzy BWM/Entropy/QFD/MULTIMOORA		Fatrias et al. [110] Charachalineur, Bauden and
	Rough BWM/MAIRCA		Cheraghalipour, Paydar and
	DIA (B.A		Hajiaghaei-Keshteli [82]
	BWM		Liu et al. [129]
	BWM		Badi and Ballem [122]
	BWM BM/M/VIKOR		Rezaei and Lajimi [59]
	BWM/VIKOR BWM/SWOT/QFD		Rezaei et al. [63] Kusi-Sarpong, Gupta and Sarkis [64]
	BWM		Liu, Hu and Zhang [84]
	DVVIVI		Vahidi, Torabi and Ramezankhani [127]
			Setyono and Sarno [69]
Manufacturing	BWM	13	Rezaei [20]
Wanuacturing	Fuzzy BWM/GMIR	15	Guo and Zhao [38]
	Fuzzy ANP/BWM		Alimohammadloua and Bonyani [114]
	QFD/PT/PHFLTS/BWM		Huang et al. [137]
	RIM/Entropy/BWM		Sofuoğlu [116]
	Interval BWM		Ren [32]
	Interval BWM		Ren et al. [77]
	Fuzzy BWM		Raj and Srivastava [145]
	Euclidean BWM		Koçak, Çağlar and Öztaş [37]
	BWM		Moktadir et al. [56]
	Fuzzy BWM/Entropy/VIKOR/FEMA		Tian et al. [138]
	BWM		Beemsterboer, Hendrix and Claassen [62]
	Interval BWM		Sadjadia and Karimi [78]
Performance evaluation	BWM		Salimi and Rezaei [35]
	FDM/VIKOR/BWM		Zhao, Zhao and Guo [120]
	ELECTRE III/PROMETHEE II/BWM	8	Bonyani and Alimohammadlou [121]
	Fuzzy BWM	-	Torbati and Sayadi [74]
	Fuzzy TOPSIS/BWM		Gupta [28]
	BWM		Bonyani and Alimohammadlou [60]
	BWM/DEA/PROMETHEE II		Alimohammadlou and Bonyani [125]
	Fuzzy BWM		Khanmohammadi, Zandieh and Tayebi
			[76]
Airline industry	VIKOR/BWM	6	Gupta [27]
	MABAC/IVFRN/BWM		Pamučar et al. [112]
	BWM		Rezaei et al. [47]
	VIKOR/TLF/BWM		Shojaei et al. [113]
	SERVQUAL/BWM		Rezaei et al. [94]
	BWM		Gupta and Barua [22]
Energy	TOPSIS/BWM	5	You et al. [79]
	BWM		Kaa et al. [55]
	Entropy method/CPT/Grey theory		Zhao, Guo and Zhao [140]
	Fuzzy BWM/TOPSIS/Taguchi method/Neutral network		Omrani, Alizadeh and Emrouznejad [130]
	FDM/Entropy weight determination/VIKOR		Zhao, Guo and Zhao [132]
Transportation	Cognitive Network Process/BWM	5	Zhang et al. [91]
	BWM		Groenendijk, Rezaei and Correia [57]
	Rough BWM/Rough WASPAS		Stević et al. [144]
	BWM		Rezaei et al. [58]
	BWM		Sharma, Mangla and Patil [61]
ducation	Fuzzy-Delphi Method/BWM	4	Nafari et al. [86]
Education	BWM		Salimi [34]
Education	Divin		Salimi and Rezaei [33]
Education	BWM		Summ und nebuer [55]
Education			Yang et al. [72]
	BWM	4	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Education Technology	BWM BWM	4	Yang et al. [72]
	BWM BWM Extension theory/Combined weights/BWM	4	Yang et al. [72] Ren [30]

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Application areas	Approaches	No of publications	References
Health care	intuitionistic fuzzy multiplicative/group decision making/BWM/GDM	3	Mou et al. [104]
	Intuitionistic fuzzy/Graph theory/BWM		Mou et al. [105]
	BWM/VIKOR		Alsalem [85]
Investment	TOPSIS/BWM	3	Askarifar et al. [80]
	Fuzzy/GDM/BWM		Hafezalkotob and Hafezalkotob [108]
	Probabilistic hesitant fuzzy BWM		Li, Wang and Hu [73]
Location selection	MAIRCA/Rough numbers and fuzzy logic/BWM	3	Pamučar et al. [109]
	ELECTRE III/GDM/BWM		You et al. [106]
	Rough BWM/Rough SAW		Stević [111]
SMEs	BWM	3	Gupta and Barua [22]
	Fuzzy TOPSIS/BWM		Gupta and Barua [25]
	Fuzzy TOPSIS/BWM		Gupta and Barua [26]
Water management	AHP/SWOT/BWM	3	Chitsaz and Azarnivand [107]
	FMEA/Linguistic distribution assessment/BWM		Nie et al. [119]
	Linguistic distribution		Nie et al. [139]
	assessment/TOPSIS/DEMATEL/BWM		
Building	BWM	2	Gupta, Anand and Gupta [23]
	COPRAS/BWM		Mahdiraji et al. [118]
Logistic	BWM	2	Rezaei et al. [54]
	Interval rough BWM/WASPAS/MABAC		Pamucara, Chatterjee and Zavadskasc
		_	[131]
Outsourcing adoption	ELECTRE/BWM	2	Yadav et al. [99]
	BWM/VIKOR	_	Garg and Sharma [83]
Sharing Arrangements	BWM	2	Praditya and Janssen [46]
.	QFD/fuzzy MULTIMOORA/fuzzy BWM		Tian et al. [135]
Turning operations	TOPSIS/Grey relational analysis/Weighted sum	2	Sofuoğlu and Orak [134]
	approach/BWM		
	BWM		Sofuoğlu et al. [92]
Verification	BWM	2	Vishnupriyan and Manoharan [65]
	BWM		Zavadskas [67]
Web service selection	AHP/Borda/BWM	2	Serrai et al. [81]
A	VIKOR/BWM		Serrai et al. [133]
Agriculture	MULTIMOORA/WASPAS/BWM	1	Hafezalkotob et al. [117]
Automotive	BWM	1	Kaa et al. [50]
Banking service	BWM	1	Yadollahi et al. [52]
Biology	BWM	1	Kaa et al. [48]
Car selection	Lexicographic semi-ordermodel (LSM)/Sensitive	1	Safarzadeh and Rasti-Barzoki [101]
Claud assurias extention	analysis Markov choice (DM/M	1	Neuron et al. [100]
Cloud service selection	Markov chains/BWM	1	Nawaz et al. [100]
Eco-industrial parks	BWM		Zhao et al. [51]
Emergency routes evaluation	2-tuple linguistic BWM/QFD	1	Mei, Liang and Tu [123]
Emotion management	BWM	1	Alhubaishy and Benedicenti [43]
Environment	BWM	1	Liu et al. [66]
Film/Movie Theater	EMSR-B/BWM	1	Joshi and Lohiya [88]
Food industry	PROMETHEE II/BWM	1 1	Alimohammadlou and Bonyani [96]
Mathematics Modical tourism	BWM SMOT/DMM		Brunelli and Rezaei [36]
Medical tourism	SW01/BWM	1	Abadi et al. [93]
Mining Mahila phone coloction	BWM	1	Ajrina, Sarno and Ginardi [68]
Mobile phone selection	BWM	1	Rezaei [1] Safarzadah, Khansofid and Pasti Parzoki
Piping selection	BWM/GDM	1	Safarzadeh, Khansefid and Rasti-Barzoki
Delverention	Internal TOPCIC/Common DIAMA	1	[102] Warr et al. [20]
Polygeneration	Interval TOPSIS/Fuzzy BWM	1	Wang et al. [29]
Product deletion	Fuzzy BWM/MACBETH	1	Pourhejazy, Sarkis and Zhu [126]
Product design	Fuzzy BWM/AD	1	Maghsoodi et al. [124]
Risk assessment	BWM	1	Torabi et al. [41] Sotoudeh-Anvari et al. [136]
Search problem	simple additive weighting/BWM	1	1
Water treatment plant	BWM/AQM/FMEA	1	Liu et al. [128]

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